# Statistical Considerations for Comparison to Background 

John W. Kern PhD.

Kern Statistical Services, Inc.
Sauk Rapids MN

## Factors Controlling Selection of Statistical Methods

- Objectives
- Baseline Comparisons
- Injury quantification
- Adaptive management triggers
- Demonstration of restoration success
- Sampling design
- Random, Systematic, Stratified, Biased
- Metric or variable types
- Continuous Variables (Sediment concentration, Biomass)
- Discrete Counts (Stem density, Species richness, Abundance)
- Binary Outcomes (Presence absence, Percent survival)
- Categorical Scores (Red green blue)
- Indices (HIS, Habitat value, Resource selection)
- Qualitative Scoring Systems
- Potential for confounding factors


## Primary Comparison of Interest for HEA (Baseline)

1) Document and estimate the duration and extent of injury, from the time of injury until the resource recovers to baseline, or possibly to a maximum level below baseline condition ${ }^{1}$.
${ }^{1}$ Habitat Equivalency Analysis: An Overview. Damage Assessment and Restoration Program National Oceanic and Atmospheric Administration Department of Commerce. Revised May 23., 2006.

## Difficulties With Site vs. Baseline Comparisons

- Baseline data may not be available for the site.
- Ecological conditions vary temporally, so baseline is often not a single condition.
- Reference sites are typically used as a surrogate for baseline, creating the potential for site vs. baseline comparisons to be confounded.


## Some Examples:

- Chromium concentration in San Diego Bay sediment.
- Sex ratios in Horseshoe Crabs at Cape Cod Bay and Monomoy National Wildlife Refuge, MA.
- Species richness in salt marsh in Hatches Harbor, MA.
- Water Quality (Surface Coal Mine, UT)
- Fish PCB Concentrations (Kalamazoo River, MI)


## Confounding Factors:

## San Diego Bay Chromium



| Site | Mean <br> $\mathrm{Cr}(\mathrm{mg} / \mathrm{kg})$ | Mean <br> \% Fines |
| :---: | :---: | :---: |
| Reference <br> $(\mathrm{N}=12)$ | 25.2 | 33.4 |
| Assessment <br> $(\mathrm{N}=66)$ | 60.3 | 68.0 |

- Percent fines may be confounded with site effects.
- This may limit the strength of the data to support regulatory decisions.
- Interpretation of data is conditioned on the effects of percent fines on Chromium concentration.


## Confounding Factors Are Often Handled Qualitatively

- From NASSCO and Southwest Marine Detailed Sediment Investigation: Volume I (Exponent Inc., October 2003):
- "Because higher chemical concentrations are ordinarily associated with finer grain sizes and higher TOC content, and because benthic macroinvertebrate community composition also depends on these variables, the physical differences between reference and shipyard stations are expected to result in different chemical and biological conditions regardless of any influences of the shipyards."


## Regression Approach To Adjust For Confounding Factors.


$C r=\beta_{0}+\beta_{1} \times$ Fines $+\beta_{2} \times$ Site $+\beta_{3} \times$ Fines $\times$ Site

## Akaike Information Criterion Can Be Used to Select Best Model.


$C r=\beta_{0}+\beta_{1} \times$ Fines $+\beta_{2} \times$ Site $+\beta_{3} \times$ Fines $\times$ Site

## Model Fit and Analysis of Parameters

| Model | AIC |
| :---: | :---: |
| Chromium $\sim$ \% Fines | 623.2 |
| Chromium $\sim$ \% Fines + Site | $\mathbf{6 1 7 . 9}$ |


|  | Estimate | Std Error | t value | $\operatorname{Pr}(>\|\mathbf{t}\|)$ |
| ---: | ---: | ---: | ---: | ---: |
| Intercept | 5.07 | 5.10 | 0.99 | 0.324 |
| \% Fines | 0.60 | 0.01 | 6.21 | $\leq 0.001$ |
| Site | 14.73 | 5.46 | 2.70 | 0.009 |

Site effect of $14.7 \mathrm{mg} / \mathrm{kg}$. $95 \% \operatorname{UCL}(13.7,25.7)$

## Pre-Post Evaluation of Cape Cod Bay Horseshoe Crabs

- Metric of Interest: Proportion of Females (Binary)
- There is an apparent decline in 2002 after an adverse event.
- Is the observed decline due to an event or due to natural temporal variation.
- It could be argued that the proportion of females in 2001 represents baseline condition.


## Reference Data From the Monomoy National Wildlife Refuge Changes the Picture (BACI)

- Temporal trends appear to be similar at Monomoy National Wildlife Refuge and Cape Cod Bay.
- Event effects are tested by looking at interaction between time and location
- Test for difference of differences.


Before After Control Impact (BACI)
With Logistic Regression

$$
\operatorname{logit}(p)=\beta_{0}+\beta_{1} x_{1}+\beta_{2} x_{2}+\beta_{3} x_{1} x_{2}
$$

$$
x_{1}=\left\{\begin{array}{c}
1 \text { for Cape Cod } \\
0 \text { for Monomoy NWR }
\end{array} ; \quad x_{2}=\left\{\begin{array}{c}
1 \text { for } 2001 \\
0 \text { for } 2000
\end{array}\right.\right.
$$

## Species Richness of Salt Marsh Vegetation Another BACI Design

Long-term Coastal Ecosystem Monitoring Program at Cape Cod National Seashore

Stewart-Oaten, A., W.W. Murdoch, and K.R. Parker. 1986. Environmental impact assessment: "pseudoreplication" in time? Ecology 67: 929-940.

Underwood, A.J. 1992. Beyond BACI: the detection of environmental impacts on populations in the real, but variable, world. J. of Experimental Marine Biology and Ecology 161: 145-178.

## Species Richness Hatches Harbor, Provincetown, MA

| Mean Species Richness |  |  |  |
| :---: | :---: | :---: | ---: |
| Year | Restricted | Unrestricted | Ratios |
| 1997 | 8.6 | 3.9 | 2.2 |
| 2000 | 9.8 | 3.3 | 3.0 |
| 2002 | 5.5 | 2.2 | 2.4 |




## Poisson Regression Model for Counts BACI Design

- Count data are typically not normally distributed when counts are "small".
- The Poisson distribution is a reasonable alternative for count data.
- Log of the mean response is assumed to be a linear function of the predictors.
- Parameter estimation based on

$$
\begin{gathered}
E(y)=\mu=e^{\beta_{0}+\beta_{1} \text { year }+\beta_{2} \text { site }+\beta_{3} \text { Year } \times \text { Site }} \\
\log (\mu)=\beta_{0}+\beta_{1} \text { Year }_{1}+\beta_{2} \text { Site }+\beta_{3} \text { Year } \times \text { Site } \\
\operatorname{prob}(Y=y)=\frac{\mu^{y} e^{-\mu}}{y!} ; y=0,1,2, \ldots
\end{gathered}
$$ maximum likelihood.

- Statistical inferences are based on the likelihood and deviance as with logistic regression.
- Over dispersion is accommodated


## BACI Analysis of Species Richness in Salt Marsh

- Richness was higher at the restricted site ( $p=0.0001$ )
- Temporal trajectories were similar at restricted and unrestricted sites.
- Verdict still out.

Mean Species Richness


| Likelihood Ratio Tests |  |  |  |
| :---: | :---: | :---: | :---: |
| Source | df | F | Significance |
| Year | 2 | 14.4 | 0.0001 |
| Study Area | 1 | 145 | 0.0001 |
| Year x Study Area | 2 | 1.4 | 0.2579 |

## Temporal Variation and Confounding Factors

## Water Quality Trends

## TDS vs Time



TDS $=\mathrm{B}_{0}+\mathrm{B}_{1}$ (Time) + Error

## Annual precipitation data are also available.

## Annual Average TDS andAnnual Precipitation vs Year



## TDS $=\mathrm{B}_{0}+\mathrm{B}_{1}($ Precip $)+\mathrm{B}_{2}$ (Time) $)$ Error




## Mean PCB Concentration and Percent Lipids in Carp Fillets (Skin Off)




## Which is Right?




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